## ASSIGNMENT 5 — FUNCTIONAL PROGRAMMING

 ${\rm COMP}\; 3010 - {\rm ORGANIZATION}\; {\rm OF}\; {\rm PROGRAMMING}\; {\rm LANGUAGES}$ 

1. LISP & SCHEME

**Exercise 1.** Consider the Scheme definition:

```
(define (mystery x y)
```

```
(lambda (z) (x (y (x z))))
```

- (1) Translate the mystery function to a  $\lambda$ -calculus expression. *HINT:* You will need  $\lambda$ s introducing the parameters x and y around the body of mystery.
- (2) What happens when you evaluate
  (mystery (lambda (x) (+ 1 x)) (lambda (y) (\* 2 y)))
- (3) What happens when you evaluate
  ((mystery (lambda (x) (+ 1 x)) (lambda (y) (\* 2 y))) 5)
- (4) What happens when you evaluate (((mystery (lambda (x) (+ 1 x)) (lambda (y) (\* 2 y))) 5) 6)

**Exercise 2.** Remember the map function, which changes every element of a list using a given operation, is written in Scheme as

so that a list (list  $x y \ldots z$ ) is transformed like so

(map f (list x y ... z)) = (list (f x) (f y) ... (f z))

reduce, which compresses a list by replacing every cons with a chosen binary operation and the final null with a chosen constant, is written in Scheme as

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(4) (Multiple Choice) Consider this definition of the function f: (define (f xs)

(reduce + 0 (map (lambda (x) (\* x x)) xs)))

Which of the following alternate definitions of f is equivalent to the one above that used map and reduce?

2. ML FAMILY

**Exercise 3.** Do Concepts In Programming Languages Exercise 5.3 on Nonlinear Pattern Matching (page 123).

*Note*, for parts (a) and (b), you can write the described functions in SML syntax as asked by the exercise, *OR* in your choice of Ruby, Python, or C syntax.

**Exercise 4.** Do *Concepts In Programming Languages* Exercise 5.7 on Disjoint Unions (page 125).

**Exercise 5.** In SML, *all* references must point to real values in the heap. In other words, SML does not support implicit null pointers in place of a reference. Instead, the SML data type declaration

datatype 'a option = NONE | SOME of 'a;

defines the generic type 'a option of references which could *either* point to nothing (represented by the NONE constructor containing no data) *or* point to some actual 'a in the heap (represented by the SOME constructor containing a value of type 'a).

For example, the integer division operation x div y will raise an exception when the divisor y is 0. A safe version of division, which never raises an exception, can be written in SML as

fun safe\_div(x, 0) = NONE

| safe\_div(x, y) = SOME(x div y);

which takes a pair of ints and returns an int option.

- (1) What is the difference between the result of evaluating 10 div 0 versus safe\_div(10, 0)?
- (2) What is the difference between the result of evaluating 10 div 5 versus safe\_div(10, 5)?
- (3) What happens when you try to evaluate 2 \* (10 div 5)? What happens when you try to evaluate 2 \* (safe\_div(10, 5))?

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